

ARMY RESEARCH LABORATORY



Formulas for the Pressure and Bulk Modulus in Uniaxial Strain

Michael J. Scheidler

ARL-TR-960

February 1996

DTIC QUALITY INSPECTED 4

19960212 125

APPROVED FOR PUBLIC RELEASE; DISTRIBUTION IS UNLIMITED.

NOTICES

Destroy this report when it is no longer needed. DO NOT return it to the originator.

Additional copies of this report may be obtained from the National Technical Information Service, U.S. Department of Commerce, 5285 Port Royal Road, Springfield, VA 22161.

The findings of this report are not to be construed as an official Department of the Army position, unless so designated by other authorized documents.

The use of trade names or manufacturers' names in this report does not constitute indorsement of any commercial product.

REPORT DOCUMENTATION PAGE			Form Approved OMB No. 0704-0188	
Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project(0704-0188), Washington, DC 20503.				
1. AGENCY USE ONLY (Leave blank)		2. REPORT DATE February 1996		3. REPORT TYPE AND DATES COVERED Final, May-July 1995
4. TITLE AND SUBTITLE Formulas for the Pressure and Bulk Modulus in Uniaxial Strain			5. FUNDING NUMBERS PR: 1L1611102AH43	
6. AUTHOR(S) Michael J. Scheidler				
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) U.S. Army Research Laboratory ATTN: AMSRL-WT-TD Aberdeen Proving Ground, MD 21005-5066			8. PERFORMING ORGANIZATION REPORT NUMBER ARL-TR-960	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)			10. SPONSORING/MONITORING AGENCY REPORT NUMBER	
11. SUPPLEMENTARY NOTES				
12a. DISTRIBUTION/AVAILABILITY STATEMENT Approved for public release; distribution is unlimited.			12b. DISTRIBUTION CODE	
13. ABSTRACT (Maximum 200 words) For an isotropic elastic solid, the pressure $p = p_u(\rho)$ in a state of uniaxial strain at density ρ generally differs from the pressure $p = p_h(\rho)$ in a state of hydrostatic stress at the same density. Several researchers have used pressure/shear (or oblique plate impact) tests to determine p_u and the corresponding uniaxial bulk modulus $K_u \equiv \rho dp_u/d\rho$. The pressure/shear tests yield uniaxial longitudinal and shear moduli, L_u and G_u , as functions of ρ . A common procedure is to integrate the approximate relation $K_u \approx L_u - 4/3 G_u$ to obtain the pressure-density relation $p = p_u(\rho)$ in uniaxial strain. It is shown here that the integration of this approximate relation between the moduli can be avoided altogether by utilizing the exact formula $p_u = \sigma_1 - 2/3 [(p/\rho_0)^2 - 1] G_u$, where σ_1 denotes the longitudinal stress (positive in compression). The bulk modulus K_u is computed exactly from this formula, and the error in approximating it by $L_u - 4/3 G_u$ is determined.				
14. SUBJECT TERMS pressure, bulk modulus, uniaxial strain			15. NUMBER OF PAGES 11	
			16. PRICE CODE	
17. SECURITY CLASSIFICATION OF REPORT UNCLASSIFIED	18. SECURITY CLASSIFICATION OF THIS PAGE UNCLASSIFIED	19. SECURITY CLASSIFICATION OF ABSTRACT UNCLASSIFIED	20. LIMITATION OF ABSTRACT UL	

INTENTIONALLY LEFT BLANK.

Table of Contents

		<u>Page</u>
1	INTRODUCTION	1
2	ACCELERATION WAVE SPEEDS	1
3	HYDROSTATIC STRESS	2
4	UNIAXIAL STRAIN	3
5	DISCUSSION	5
6	REFERENCES	7
	DISTRIBUTION LIST	9

INTENTIONALLY LEFT BLANK.

1 INTRODUCTION

We consider only isotropic elastic materials, and for simplicity thermal effects are neglected until §5. Under these conditions, the pressure is typically assumed to be a function of density only. However, nonlinear elasticity theory predicts that the pressure also depends on the shear strain, although isotropy implies this effect is necessarily of second order; cf. Scheidler [1]. In §4 we derive exact formulas for the pressure and bulk modulus in a state of uniaxial strain. The effect of shear strain can be seen by comparing these results with the corresponding relations for a state of hydrostatic stress (§3). Our results are based on exact formulas for the speeds of acceleration waves (§2). Applications to the analysis of data from pressure/shear tests are discussed in §5.

2 ACCELERATION WAVE SPEEDS

Let \mathbf{F} denote the deformation gradient relative to the undeformed and unstressed state. The left Cauchy-Green tensor $\mathbf{B} \equiv \mathbf{F}\mathbf{F}^T$ has principal values $b_i = \lambda_i^2$, where λ_i are the principal stretches, and

$$\det \mathbf{F} = \sqrt{b_1 b_2 b_3} = \lambda_1 \lambda_2 \lambda_3 = \frac{1}{\tilde{\rho}}, \quad \tilde{\rho} \equiv \frac{\rho}{\rho_0}, \quad (2.1)$$

where ρ and ρ_0 denote the densities in the deformed and undeformed state. The principal axes of \mathbf{B} are the principal axes of strain in the deformed state. Since the material is isotropic and elastic, these axes are also the principal axes of the Cauchy stress tensor \mathbf{T} , and \mathbf{T} is an isotropic function of \mathbf{B} . This implies that there is a single function \hat{t} such that the principal stresses t_i are given by

$$t_i = \hat{t}(b_i, b_j, b_k) = \hat{t}(b_i, b_k, b_j), \quad (2.2)$$

for any permutation i, j, k of 1, 2, 3; cf. Truesdell & Noll [2, §48]. It follows that the pressure

$$p \equiv -\frac{1}{3} \text{tr } \mathbf{T} = -\frac{1}{3}(t_1 + t_2 + t_3) \quad (2.3)$$

is a symmetric function of b_1, b_2, b_3 . Analogous results hold in terms of the principal stretches λ_i or in terms of various principal strain measures, e.g., $\lambda_i - 1$, $\frac{1}{2}(b_i - 1)$, $\frac{1}{2}(1 - 1/b_i)$, or $\ln \lambda_i$.

The speed U_i of a longitudinal acceleration wave propagating along the i th principal axis of strain is given by

$$\rho U_i^2 = 2b_i \frac{\partial t_i}{\partial b_i} = \lambda_i \frac{\partial t_i}{\partial \lambda_i} = \frac{\partial t_i}{\partial \ln \lambda_i}. \quad (2.4)$$

The speed U_{ij} of a transverse (or shear) acceleration wave propagating along the i th principal axis of strain with jump in acceleration parallel to the j th principal axis ($j \neq i$) is given by Ericksen's formula:

$$\begin{aligned}\rho U_{ij}^2 &= b_i \left(\frac{\partial t_i}{\partial b_i} - \frac{\partial t_i}{\partial b_j} \right), \quad \text{if } b_i = b_j, \\ &= b_i \frac{t_i - t_j}{b_i - b_j}, \quad \text{if } b_i \neq b_j.\end{aligned}\tag{2.5}$$

All quantities in (2.4) and (2.5) are evaluated at the wave front. These wave speeds are in the deformed material (i.e., Eulerian); the corresponding Lagrangian wave speeds are obtained by dividing by λ_i . Proofs of (2.4) and (2.5) can be found in Truesdell & Noll [2, §74] and Wang & Truesdell [3, §VI.5]. These formulae do not require that the region ahead of the wave be at rest or in a homogeneous state of strain. However, when these conditions are satisfied, (2.4) and (2.5) also apply to the speeds of plane infinitesimal sinusoidal waves; cf. Truesdell & Noll [2, §73].

3 HYDROSTATIC STRESS

For a purely dilatational deformation, we have

$$b_i = \tilde{\rho}^{-2/3} \quad \text{and} \quad t_i = -p \quad (i = 1, 2, 3).\tag{3.1}$$

In this hydrostatic stress state, every axis is a principal axis of stress and strain, and the pressure p is a function p_h of ρ or $\tilde{\rho}$. Here and below, an "h" subscript denotes the hydrostatic stress state. From (2.2), (2.4), (2.5)₁, and (3.1), it follows that for a given density ρ there is a single longitudinal wave speed $U_i = U_{L,h}$ and a single shear wave speed $U_{ij} = U_{S,h}$, and that

$$\frac{dp_h}{d\rho} = U_{L,h}^2 - \frac{4}{3}U_{S,h}^2;\tag{3.2}$$

cf. Wang & Truesdell [3, §VI.5]. A different proof of this well-known result is given by Truesdell & Noll [2, §75]. We assume p_h is a strictly increasing function of ρ . Then (3.2) implies the longitudinal wave speed is greater than the shear wave speed. With the longitudinal, shear, and bulk moduli defined by

$$L_h \equiv \rho U_{L,h}^2 \quad G_h \equiv \rho U_{S,h}^2\tag{3.3}$$

$$K_h \equiv \rho \frac{dp_h}{d\rho} = \tilde{\rho} \frac{dp_h}{d\tilde{\rho}},\tag{3.4}$$

(3.2) implies the well-known relation

$$K_h = L_h - \frac{4}{3}G_h.\tag{3.5}$$

We use a zero subscript to denote functions evaluated at the undeformed and unstressed state where $\lambda_i = b_i = \tilde{\rho} = 1$; in particular, $K_0 = L_0 - \frac{4}{3}G_0$. By (3.4),

$$p_h/K_0 \approx (\tilde{\rho} - 1) + a_0(\tilde{\rho} - 1)^2, \quad (3.6)$$

where the dimensionless constant a_0 is given by

$$a_0 = \frac{1}{2K_0} \left. \frac{d^2 p_h}{d\tilde{\rho}^2} \right|_0 = \frac{1}{2} \left(\left. \frac{dK_h}{dp_h} \right|_0 - 1 \right). \quad (3.7)$$

4 UNIAXIAL STRAIN

For a state of uniaxial strain along the 1-axis,

$$\lambda_1 = \sqrt{b_1} = 1/\tilde{\rho}, \quad \lambda_2 = \lambda_3 = b_2 = b_3 = 1, \quad (4.1)$$

and (2.2) implies $t_2 = t_3$. The principal stresses t_i are positive in tension; if $\sigma_i \equiv -t_i$ then σ_i is positive in compression. We use a "u" subscript to denote uniaxial strain and consider only waves propagating along the 1-axis into a uniaxially strained material. The Eulerian wave speed $U_{L,u} = U_1$ of a longitudinal acceleration wave is given by (2.4) with $i = 1$, and by (4.1) we also have

$$L_u \equiv \rho U_{L,u}^2 = \tilde{\rho} \frac{d\sigma_1}{d\tilde{\rho}} = \rho \frac{d\sigma_1}{d\rho}. \quad (4.2)$$

It follows that a longitudinal acceleration wave can propagate only if $d\sigma_1/d\tilde{\rho} > 0$, i.e., if σ_1 is a strictly increasing function of $\tilde{\rho}$, which we now assume. By (4.1), the material is strained iff $\tilde{\rho} \neq 1$ iff $b_1 \neq b_2$. In this case (2.5)₂ and (4.1) imply the following formulas for the Eulerian speed $U_{S,u} = U_{12}$ of a transverse or shear acceleration wave:

$$\begin{aligned} G_u \equiv \rho U_{S,u}^2 &= b_1 \frac{t_1 - t_2}{b_1 - b_2} = \frac{t_1 - t_2}{1 - \tilde{\rho}^2} \\ &= \frac{\sigma_1 - \sigma_2}{\tilde{\rho}^2 - 1} = \frac{2\tau}{\tilde{\rho}^2 - 1}, \end{aligned} \quad (4.3)$$

where τ is the shear stress:

$$\tau \equiv \frac{1}{2}(\sigma_1 - \sigma_2) = \frac{1}{2}(t_2 - t_1). \quad (4.4)$$

The Lagrangian wave speeds are $\tilde{\rho} U_{L,u}$ and $\tilde{\rho} U_{S,u}$. If $\tilde{\rho} > 1$ the material is in compression, and (4.3) implies that a shear acceleration wave can propagate only if $\sigma_1 > \sigma_2$. When $\tilde{\rho} = 1$, the results of the previous section apply, and we have $G_u|_0 = G_0$ and $L_u|_0 = L_0$.

From (4.3) we have the following fundamental formula for the shear stress in uniaxial strain:

$$\tau = \frac{1}{2}(\tilde{\rho}^2 - 1)G_u. \quad (4.5)$$

Since $t_2 = t_3$, (2.3) and (4.4) imply the following well-known relation between the (compressive) longitudinal stress σ_1 , the shear stress τ , and the pressure p_u in uniaxial strain:

$$p_u = \sigma_1 - \frac{4}{3}\tau. \quad (4.6)$$

On substituting (4.5) into (4.6), we obtain the following fundamental formula for p_u :

$$p_u = \sigma_1 - \frac{2}{3}(\tilde{\rho}^2 - 1)G_u. \quad (4.7)$$

We define the bulk modulus K_u in uniaxial strain by

$$K_u \equiv \rho \frac{dp_u}{d\rho} = \tilde{\rho} \frac{dp_u}{d\tilde{\rho}} = L_u \frac{dp_u}{d\sigma_1}. \quad (4.8)$$

Then from (4.7) and (4.2), we obtain

$$\begin{aligned} K_u &= L_u - \frac{4}{3}\tilde{\rho}^2 G_u - \frac{2}{3}(\tilde{\rho}^2 - 1)\tilde{\rho} \frac{dG_u}{d\tilde{\rho}} \\ &= (L_u - \frac{4}{3}G_u) - \frac{2}{3}(\tilde{\rho}^2 - 1)H_u, \end{aligned} \quad (4.9)$$

$$H_u = 2G_u + \tilde{\rho} \frac{dG_u}{d\tilde{\rho}} = \frac{1}{\tilde{\rho}} \frac{d}{d\tilde{\rho}}(\tilde{\rho}^2 G_u). \quad (4.10)$$

At $\tilde{\rho} = 1$, (4.9) reduces to $K_u|_0 = L_0 - \frac{4}{3}G_0 = K_0$. From (4.9) and (4.10) it follows that $K_u = L_u - \frac{4}{3}G_u$ for all $\tilde{\rho}$ iff $H_u = 0$ iff $G_u = G_0/\tilde{\rho}^2$, but there is no reason to expect such dependence in general, and thus no reason to expect that $K_u = L_u - \frac{4}{3}G_u$ except in the limit of zero strain. Of course, by analogy with (3.5) we could have defined K_u to be $L_u - \frac{4}{3}G_u$, but then (4.8) would not hold. From (4.9) we see that for a state of compression, $K_u < L_u - \frac{4}{3}G_u$ if $H_u > 0$, and $K_u > L_u - \frac{4}{3}G_u$ if $H_u < 0$. We assume that p_u is a strictly increasing function of $\tilde{\rho}$. Then any function of $\tilde{\rho}$ may also be regarded as a function of σ_1 or p_u , and by (4.2) and (4.8) we have

$$\rho \frac{d}{d\rho} = \tilde{\rho} \frac{d}{d\tilde{\rho}} = L_u \frac{d}{d\sigma_1} = K_u \frac{d}{dp_u}. \quad (4.11)$$

The results up to this point are exact. We now consider some useful approximate relations. From (4.8) we have

$$p_u/K_0 \approx (\tilde{\rho} - 1) + b_0(\tilde{\rho} - 1)^2, \quad (4.12)$$

where the dimensionless constant b_0 is given by

$$b_0 = \frac{1}{2K_0} \left. \frac{d^2 p_u}{d\tilde{\rho}^2} \right|_0 = \frac{1}{2} \left(\left. \frac{dK_u}{dp_u} \right|_0 - 1 \right). \quad (4.13)$$

For use in (4.12)–(4.13), note that (4.9) implies

$$\left. \frac{dK_u}{dp_u} \right|_0 = \frac{L_0}{K_0} \left(\left. \frac{dL_u}{d\sigma_1} \right|_0 - \frac{8}{3} \left. \frac{dG_u}{d\sigma_1} \right|_0 \right) - \frac{8}{3} \frac{G_0}{K_0}. \quad (4.14)$$

From (3.6)–(3.7) and (4.12)–(4.13), we see that

$$p_u \approx p_h + K_0 c_0 (\tilde{\rho} - 1)^2, \quad (4.15)$$

$$\frac{p_u - p_h}{p_u} \approx \frac{p_u - p_h}{p_h} \approx c_0 (\tilde{\rho} - 1), \quad (4.16)$$

where the dimensionless constant c_0 is given by

$$c_0 = b_0 - a_0 = \frac{1}{2} \left(\left. \frac{dK_u}{dp_u} \right|_0 - \left. \frac{dK_h}{dp_h} \right|_0 \right). \quad (4.17)$$

On comparing (4.16) with equation (4.6) in Scheidler [1], we find that c_0 is also given by

$$c_0 = \frac{2}{3} \left(\left. \frac{dG_h}{dp_h} \right|_0 - \frac{G_0}{K_0} \right). \quad (4.18)$$

5 DISCUSSION

The longitudinal stress σ_1 as a function of $\tilde{\rho}$ in uniaxial strain can be obtained from normal plate impact tests. Then the relation (4.6) (which does not rely on the assumption that the response is elastic) is typically used to determine the pressure p_u in uniaxial strain given some assumptions on the shear stress τ , or to determine τ given some assumptions on p_u . It is often assumed that $p_u(\tilde{\rho})$ is equal to the pressure $p_h(\tilde{\rho})$ in a state of hydrostatic stress at density $\tilde{\rho}$ (or to some appropriate modification of p_h to include thermal effects in the shocked state). Such an approximation neglects the effects of shear strain (or shear stress) on p_u . That this effect may be significant in ceramics, geologic materials, and polymers has been emphasized by Gupta [4] and Conner [5]. These materials can sustain relatively large elastic shear strains (compared to metals), although for polymers viscoelastic effects should also be taken into account. Only elastic response is considered here. Then (4.15) implies that $p_u(\tilde{\rho})$ differs from $p_h(\tilde{\rho})$ by a term of order $(\tilde{\rho} - 1)^2$ unless $c_0 = 0$, which is generally not the case. If c_0 and $p_h(\tilde{\rho})$ are known, then (4.15) provides an approximation to p_u to within an error of order $(\tilde{\rho} - 1)^3$. The relative error in approximating p_u by p_h is of order $\tilde{\rho} - 1$ and can be estimated by using (4.16).

In a pressure/shear (or oblique plate impact) test, a longitudinal wave propagates into the undeformed material, bringing it to a state of uniaxial strain, and a slower shear wave propagates into this uniaxially strained material. These tests yield both $\sigma_1(\tilde{\rho})$ and the shear wave speed U_{Su} (and hence G_u) as a function of $\tilde{\rho}$ or σ_1 . If

the shear wave travels at the acceleration wave speed, then (4.5), (4.7), and (4.9) provide *exact* formulas for the shear stress τ , the pressure p_u , and the bulk modulus K_u in uniaxial strain as a function of $\tilde{\rho}$ or σ_1 . These formulas appear to have gone unnoticed, however. Instead, it is usually assumed that $K_u \approx L_u - \frac{4}{3}G_u$. This approximate relation, together with (4.8), is then integrated to give p_u as a function of $\tilde{\rho}$; cf. Gupta [4, 6], Conner [5], and Aidun & Gupta [7]. For fused silica in the strain range $0 \leq \tilde{\rho} - 1 \leq 0.076$, the response is elastic and the shear wave speed decreases with $\tilde{\rho}$; cf. Conner [5]. In this strain range the shear wave is an acceleration wave (cf. also Abou-Sayed & Clifton [8]), so we may apply the results of §4. Using (4.9) and Conner's data, we find that at a strain of $\tilde{\rho} - 1 = 0.076$ the estimate $K_u \approx L_u - \frac{4}{3}G_u$ is low by about 29%.

Whether the shear wave in a pressure/shear test is an acceleration wave or a shock wave depends on the nonlinear elastic response of the material; cf. Davison [9]. The shear modulus G_u in §4 is defined in terms of the acceleration wave speed $U_{S,u}$, or equivalently, in terms of the speed of a plane infinitesimal sinusoidal shear wave; cf. §2. If a shear shock with speed \bar{U} can propagate in the uniaxially strained material and if we set $\bar{G} \equiv \rho \bar{U}^2$, then the formulas in §4 hold approximately when G_u is replaced with \bar{G} . Also note that if $\bar{U} > U_{S,u}$ (as standard stability arguments would imply), then $\bar{G} > G_u$, and (4.5) and (4.7) imply that $\tau < \frac{1}{2}(\tilde{\rho}^2 - 1)\bar{G}$ and $p_u > \sigma_1 - \frac{2}{3}(\tilde{\rho}^2 - 1)\bar{G}$ in compression ($\tilde{\rho} > 1$).

We conclude with a brief discussion of thermodynamic effects, which have been neglected up to this point. If a thermoelastic material conducts heat by Fourier's law [respectively, is a nonconductor], then a longitudinal acceleration wave propagates at the isothermal [respectively, adiabatic] wave speed. However, the formula (4.3) for the speed of a shear acceleration continues to hold in either case; cf. Bowen & Wang [10]. In fact, it can be shown that (4.3) holds even if heat conduction is governed by Cattaneo's equation, which prohibits instantaneous propagation of thermal disturbances. Thus the formulas (4.5) and (4.7) for the shear stress and the pressure continue to hold. In particular, they are valid when the state of uniaxial strain has been achieved by shock loading.

6 REFERENCES

- [1] Scheidler, M. "On the Coupling of Pressure and Deviatoric Stress in Hyperelastic Materials." *Proceedings of the 13th Army Symposium on Solid Mechanics*, edited by S.-C. Chou, F. D. Bartlett, T. W. Wright, and K. Iyer, pp. 539–550, 1993.
- [2] Truesdell, C., and W. Noll. "The Non-Linear Field Theories of Mechanics." *Handbuch der Physik*, edited by S. Flügge, vol. III, no. 3, Springer, Berlin, 1965.
- [3] Wang, C.-C., and C. Truesdell. *Introduction to Rational Elasticity*. Noordhoff, Leyden, 1973.
- [4] Gupta, Y. M. "Determination of the Impact Response of PMMA Using Combined Compression and Shear Loading." *Journal of Applied Physics*, vol. 51, pp. 5352–5361, 1980.
- [5] Conner, M. P. "Shear Wave Measurements to Determine the Nonlinear Elastic Response of Fused Silica Under Shock Loading." Master's thesis, Washington State University, Pullman, 1988.
- [6] Gupta, Y. M. "Shear and Compression Wave Measurements in Shocked Polycrystalline Al_2O_3 ." *Journal of Geophysical Research*, vol. 88, pp. 4304–4312, 1983.
- [7] Aidun, J. B., and Y. M. Gupta. "Shear Wave Measurements for Improved Characterization of Shock-Induced Phase Transformations in Carrara Marble." *Geophysical Research Letters*, vol. 16, pp. 191–194, 1989.
- [8] Abou-Sayed, A. S., and R. J. Clifton. "Pressure Shear Waves in Fused Silica." *Journal of Applied Physics*, vol. 47, pp. 1762–1770, 1976.
- [9] Davison L. "Propagation of Plane Waves of Finite Amplitude in Elastic Solids." *Journal of Mechanics and Physics of Solids*, vol. 14, pp. 249–270, 1966.
- [10] Bowen, R. M., and C.-C. Wang. "Thermodynamic Influences on Acceleration Waves in Inhomogeneous Isotropic Elastic Bodies With Internal State Variables." *Archive for Rational Mechanics and Analysis*, vol. 41, pp. 287–318, 1971.

INTENTIONALLY LEFT BLANK.

<u>NO. OF COPIES</u>	<u>ORGANIZATION</u>
2	DEFENSE TECHNICAL INFO CTR ATTN DTIC DDA 8725 JOHN J KINGMAN RD STE 0944 FT BELVOIR VA 22060-6218

1	DIRECTOR US ARMY RESEARCH LAB ATTN AMSRL OP SD TA 2800 POWDER MILL RD ADELPHI MD 20783-1145
---	---

3	DIRECTOR US ARMY RESEARCH LAB ATTN AMSRL OP SD TL 2800 POWDER MILL RD ADELPHI MD 20783-1145
---	---

1	DIRECTOR US ARMY RESEARCH LAB ATTN AMSRL OP SD TP 2800 POWDER MILL RD ADELPHI MD 20783-1145
---	---

ABERDEEN PROVING GROUND

5	DIR USARL ATTN AMSRL OP AP L (305)
---	---------------------------------------

**NO. OF
COPIES ORGANIZATION**

1 SANDIA NATIONAL LABORATORIES
EXPERIMENTAL IMPACT PHYSICS DEPT 1433
ATTN D GRADY
ALBUQUERQUE NM 87185

1 BROWN UNIVERSITY
DIVISION OF ENGINEERING BOX D
ATTN R CLIFTON
PROVIDENCE RI 02912

ABERDEEN PROVING GROUND

DIR, USARL

ATTN: AMSRL-WT-T, T. WRIGHT

AMSRL-WT-TD,

J. WALTER

P. KINGMAN

S. SCHOENFELD

M. RAFTENBERG

S. SEGLETES

K. FRANK

AMSRL-MA-PD,

S.-C. CHOU

D. DANDEKAR

P. BARTKOWSKI

A. RAJENDRAN

T. WEERASOORIYA

USER EVALUATION SHEET/CHANGE OF ADDRESS

This Laboratory undertakes a continuing effort to improve the quality of the reports it publishes. Your comments/answers to the items/questions below will aid us in our efforts.

1. ARL Report Number ARL-TR-960 Date of Report February 1996
2. Date Report Received _____
3. Does this report satisfy a need? (Comment on purpose, related project, or other area of interest for which the report will be used.) _____

4. Specifically, how is the report being used? (Information source, design data, procedure, source of ideas, etc.) _____

5. Has the information in this report led to any quantitative savings as far as man-hours or dollars saved, operating costs avoided, or efficiencies achieved, etc? If so, please elaborate. _____

6. General Comments. What do you think should be changed to improve future reports? (Indicate changes to organization, technical content, format, etc.) _____

CURRENT
ADDRESS

Organization

Name

Street or P.O. Box No.

City, State, Zip Code

7. If indicating a Change of Address or Address Correction, please provide the Current or Correct address above and the Old or Incorrect address below.

OLD
ADDRESS

Organization

Name

Street or P.O. Box No.

City, State, Zip Code

(Remove this sheet, fold as indicated, tape closed, and mail.)
(DO NOT STAPLE)

DEPARTMENT OF THE ARMY

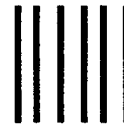
OFFICIAL BUSINESS

BUSINESS REPLY MAIL

FIRST CLASS PERMIT NO 0001,APG,MD

POSTAGE WILL BE PAID BY ADDRESSEE

**DIRECTOR
U.S. ARMY RESEARCH LABORATORY
ATTN: AMSRL-WT-TD
ABERDEEN PROVING GROUND, MD 21005-5066**



**NO POSTAGE
NECESSARY
IF MAILED
IN THE
UNITED STATES**

